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# LIST OF PUBLISHED/COMMUNICATED/PREPRINT ARTICLES

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## Journal Articles/Preprints

1. **M. Pandey**, T. Som, and S. Verma, “Fractal dimension of Katugampola fractional integral of vector-valued functions,” *The European Physical Journal Special Topics*, vol. 230, no. 21, pp. 3807–3814, 2021. doi: [10.1140/epjs/s11734-021-00327-2](https://doi.org/10.1140/epjs/s11734-021-00327-2).
2. **M. Pandey**, V. Agrawal, and T. Som, “Fractal dimension of multivariate  $\alpha$ -fractal functions and approximation aspects,” *Fractals*, vol. 30, no. 07, pp. 1–17, 2022. doi: [10.1142/S0218348X22501493](https://doi.org/10.1142/S0218348X22501493).
3. **M. Pandey**, T. Som, and S. Verma, “Set-valued  $\alpha$ -fractal functions,” *Constructive Approximation*, pp. 1–29, 2023. doi: [10.1007/s00365-023-09652-2](https://doi.org/10.1007/s00365-023-09652-2).
4. V. Agrawal, **M. Pandey**, and T. Som, “Box dimension and fractional integrals of multivariate  $\alpha$ -fractal interpolation functions,” *Mediterranean Journal of Mathematics*, vol. 20, no. 164, 2023. doi: [10.1007/s00009-023-02368-4](https://doi.org/10.1007/s00009-023-02368-4).
5. S. Verma, **M. Pandey**, and T. Som, “Some measure-theoretic aspects of fractal functions: Invariant measures and function spaces,” *Communicated*, 2023.
6. J. Sarkar, **M. Pandey**, T. Som, and B. Choudhury, “Generalized Hausdorff metric on  $S_b$ -metric space and some fixed point results,” *arXiv preprint arXiv:2303.02619*, 2023.

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1. **M. Pandey**, T. Som, and S. Verma, “Dimensional Analysis of Mixed Riemann-Liouville Fractional Integral of Vector-Valued Functions,” in *Applied Analysis, Optimization and Soft Computing, Varanasi*, India, 2021. [url: ICNAAO2021](#).
2. **M. Pandey**, V. Agrawal, and T. Som, “Some Remarks on Multivariate Fractal Approximation,” in *Frontiers of Fractal Analysis Recent Advances and Challenges*, CRC Press, pp. 1–24.