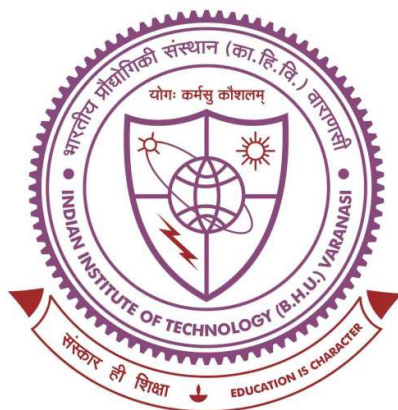


***Mie Scattering Algorithms for interaction of
structured laser beams with nanoparticles:
Modeling & Analysis***



A thesis submitted in partial fulfillment for the

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Doctor of Philosophy

in

Physics

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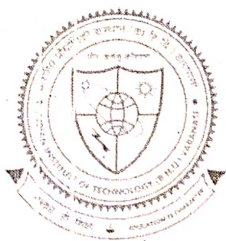
Sarita

DEPARTMENT OF PHYSICS

**INDIAN INSTITUTE OF TECHNOLOGY
(BANARAS HINDU UNIVERSITY)
VARANASI – 221005**

**Roll Number
19171012**

**Year of Submission
2024**



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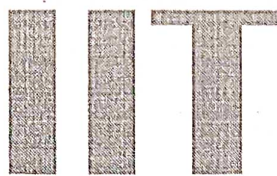
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Supervisor

Prof. Rakesh Kumar Singh
Department of Physics
Indian Institute of Technology
(Banaras Hindu University)
Varanasi-221005 (U.P), India



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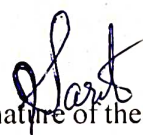
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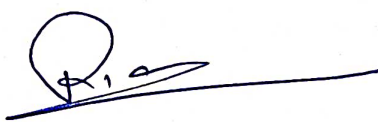
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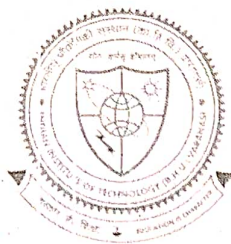

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Prof. Rakesh Kumar Singh
Professor
Department of Physics
Indian Institute of Technology
(Banaras Hindu University)
Varanasi-221005


Signature of Head of Department
Prof. Sandip Chatterjee
HEAD/विभागाध्यक्ष
भौतिकी विभाग/Deptt. of Physics
भा0प्रौ0सं0/(का0हि0वि0)/IIT (BHU)
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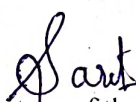
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*Success or Failure is just a state of mind, I am here to learn, and I am doing so...
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Sarita

Table of contents

Certificate	ii
Declaration by the candidate	iii
Copyright transfer certificate	iv
Acknowledgments	v
Table of contents	ix
List of figures.....	xi
Chapter 1	23
Introduction.....	23
1.1 Nanophotonics: Light-matter interaction at nanoscale	25
1.2 Plasmonic Nanostructures.....	27
1.2.1 Surface Plasmon Resonance	28
1.2.2 Localized Surface Plasmon Resonance	30
1.3 Different plasmon-assisted nanoparticles	32
1.3.1 Monometallic/Uncoated nanoparticles	32
1.3.2 Core-shell/coated nanoparticles	33
1.4 Scattering of Light	34
1.4.1 Mie Theory and Multipole Expansion	36
1.4.2 Observations based on the plasmonic response of the nanoparticles	39
1.5 Plasmonic response and near-field intensity enhancement.....	41
1.6 Motivation.....	43
1.6.1 Structured Laser Beams	44
1.7 Algorithms and commercially available tools	48
1.7.1 Available software and coding tools.....	48
1.7.2 Modeling.....	49
1.8 Applications	50
1.8.1 Surface enhanced Raman Spectroscopy	50
1.8.2 Mie Scattering Algorithm	51
1.8.2.1 Optimal measurement of water droplet size	52
1.8.2.2 Coal mine dust concentration measurement	52
Chapter 2	55
Plasmonic response of nanoparticles under Plane wave illumination	55
2.1 Introduction: Mie Scattering Theory	57
2.1.1 Monometallic nanoparticle	60
2.1.2 Core-shell nanoparticles.....	61
2.3 Mie Scattering Algorithm for a Plane Wave.....	63
2.2 Near-field Intensity Enhancement	65
2.4 Results using COMSOL Simulation.....	66
2.5 Results and Discussion: MATLAB Simulations	67

2.5.1 Monometallic/Uncoated nanoparticles	68
2.5.2 Core-shell nanoparticles.....	71
2.5 Conclusion	75
Chapter 3	77
Interaction of a tightly focused linearly polarized beam with a nanoparticle.....	77
3.1 Introduction: Tightly focused beams	79
3.2 Mie Scattering Algorithm for a tightly focused linearly polarized beam	84
3.3 Near field Intensity Enhancement.....	86
3.4 Results and Discussion	87
3.4.1 Monometallic nanoparticles.....	88
3.4.2 Core-shell nanoparticles.....	92
3.5 Conclusion	96
Chapter 4	99
Interaction of a tightly focused radially polarized beam with a nanoparticle.....	99
4.1 Introduction: Radially Polarized Tightly Focused Beams	101
4.2 Mie scattering Algorithm for a tightly focused radially polarized beam.....	103
4.3 Near field Intensity Enhancement.....	104
4.3 Results and Discussion	105
4.3.1 Monometallic nanoparticles.....	106
4.3.2 Core-shell nanoparticles.....	115
4.4 Conclusion	122
Chapter 5	123
Effects of spherical aberration and defocusing on the near-field enhancement	123
5.1 Optical aberration.....	125
5.2 Wave aberrations and Zernike polynomial	129
5.3 Mie Scattering for a tightly focused linearly polarized beam under spherical aberration and defocusing	132
5.4 Near-field intensity enhancement for an aberrated system.....	133
5.5 Results and Discussion	134
5.6 Conclusion	151
Chapter 6	153
Conclusion	153
6.1 Conclusion	155
6.2 Future plan	157
References:.....	167
List of Publications:	181

List of figures

Fig. 1.1 Gold (Au) metal at different length scales [3].	25
Fig. 1.2 Various nanostructures [11].	26
Fig. 1.3 Surface plasmon polariton.	28
Fig. 1.4 Localized surface plasmon polaritons.	31
Fig. 1.5 Monometallic (a) Au, (b) Ag nanoparticles.	33
Fig. 1.6 Core-shell nanoparticles (a) Ag@Au nanoparticle, (b) Au@Ag nanoparticle.	34
Fig. 1.7 Scattering of light in nature.	35
Fig. 1.8 Mie Scattering.	37
Fig. 1.9 Plasmonic response of a nanoparticle leading to enhancement in the near-field.	42
Fig. 1.10 Beam profile for a (a) Linear, (b) Circular, (c) Elliptical, (d) radial, and (e) Azimuthal Polarization.	45
Fig. 1.11 (a) A Polarizer converting randomly polarized light into linearly polarized light [96], (b) a circularly polarized, and (c) an elliptically polarized light produced using a Quarter waveplate [97], and (e), (f) a S-waveplate used to produce radially polarized and azimuthally polarized light respectively [98].	46
Fig. 1.12 Structure of a focal spot in low NA, and high NA focusing system. Variation in focal spot based on polarization of incident beam in high NA focusing system.	47
Fig. 1.13 Structured laser illumination in Surface Enhanced Raman Spectroscopy.	51
Fig. 1.14 Optical measurement of water droplet size using Mie Scattering theory [125, 126].	52
Fig. 1.15 Coal mine dust concentration optical sensor designed using Mie Scattering theory [127].	53
Fig. 2.1 Wave vectors corresponding to (a) monometallic and (b) core-shell nanoparticle.	61
Fig. 2.2 Linearly polarized (red arrows show the orientation of electric field vector) plane wave scattering through a nanoparticle	64
Fig. 2.3 COMSOL Multiphysics Simulation results: Normalized enhanced field (a)x-y axis, (b) y-z axis, (c) x-z axis in the near-field, and (d) far-field view for an Ag nanoparticle of 50 nm radius at $\lambda = 400 \text{ nm}$.	67
Fig. 2.4 Average radial (Kr) and tangential (Kt) intensity enhancement for a linearly polarized plane wave scattering from (a) Au, (b) Ag monometallic nanoparticles ($r = 50 \text{ nm}$) in dielectric media air, and glass.	68
Fig. 2.5 Average radial intensity enhancement (Kr) for an incident plane wave scattering from an Au nanoparticle in dielectric media (a) air, (b) glass.	69
Fig. 2.6 Average radial intensity enhancement (Kr) for an incident plane wave scattering from an Ag nanoparticle in dielectric media (a) air, (b) glass.	70
Fig. 2.7 Average radial intensity enhancement in case of an incident linearly polarized PW interacting with (a) an uncoated Au (b) an uncoated Ag, (c) Ag@Au, and (d) Au@Ag	

nanoparticles in different dielectric media air (black), BK7 (glass) ($\cdots$ red), and silicon ($- - -$ blue).	72
Fig. 2.8 Average radial intensity enhancement for an incident linearly polarized plane wave interacting with an Au@Ag nanoparticle of variable overall radius ranging from 20 nm to 100 nm and in different dielectric media (a) air, (b) BK7 (glass), and (c) silicon.....	74
Fig. 3.1 Some features of a tightly focused or a high NA beam.....	80
Fig. 3.2 Intensity distribution of the Gaussian beam focused by an aplanatic lens with $\alpha = 75^\circ$ for (a) linear, (b) radial, (c) azimuthal polarization, and with (d) $\alpha = 30^\circ$ for linear polarization [100].	81
Fig. 3.3 Electric field components for a tightly focused linearly polarized beam at the focal plane (a) $E_x(x, y)$, (b) $E_y(x, y)$, and (c) $E_z(x, y)$. The results are normalized with the maximum value of the total absolute value of the electric field.	81
Fig. 3.4 Geometric configuration of focused rays at the focal plane.	82
Fig. 3.5 A linearly polarized tightly focused beam interacting with a nanoparticle kept at the focus.....	86
Fig. 3.6 Average radial (Kr) and tangential (Kt) intensity enhancement for a tightly focused linearly polarized beam scattering from (a) Au, (b) Ag monometallic nanoparticles ($r = 50\text{ nm}$) in dielectric media air, and glass.	89
Fig. 3.7 Average radial intensity enhancement for an Ag nanoparticle in glass in low NA ($\alpha = 10^\circ, 30^\circ$), and high NA ($\alpha = 60^\circ$) focused beam with linear polarization.	90
Fig. 3.8 Average radial intensity enhancement for an incident tightly focused linearly polarized beam scattering from an Au nanoparticle in dielectric media (a) air, (b) glass.	91
Fig. 3.9 Average radial intensity enhancement for an incident tightly focused linearly polarized beam scattering from an Ag nanoparticle in dielectric media (a) air, (b) glass.	92
Fig. 3.10 Average radial intensity enhancement in case of an incident tightly focused linearly polarized beam interaction with (a) uncoated Au, (b) uncoated Ag, (c) Ag@Au, (d) Au@Ag nanoparticles in different dielectric media air (black), BK7 (glass) ($\cdots$ red), and silicon ($- - -$ blue).	94
Fig. 3.11 Average radial intensity enhancement for an incident tightly focused linearly polarized beam interacting with a Au@Ag NP of variable overall radius ranging from 20 nm to 100 nm and in different dielectric media (a) air (b) BK7 (glass), and (c) silicon.....	95
Fig. 4.1 Electric field components of a tightly focused radially polarized beam at the focal plane (a) $E_x(x, y)$, (b) $E_y(x, y)$, and (c) $E_z(x, y)$. The results are normalized with the maximum value of the total absolute value of the electric field.	102
Fig. 4.2 Tightly focused radially polarized beam illuminating a nanoparticle kept at focus.	105
Fig. 4.3 Average radial intensity enhancement for an incident tightly focused radially polarized beam scattering from an Au nanoparticle in dielectric media (a) air, (b) glass.	106
Fig. 4.4 Average radial intensity enhancement for an incident tightly focused radially polarized beam scattering from an Ag nanoparticle in dielectric media (a) air, (b) glass.	107
Fig. 4.5 Average radial intensity enhancement for an Au nanoparticle in air ($nm = 1.00$) illuminated by a linearly polarized plane wave (black); tightly focused linearly polarized beam	

(dashed red); tightly focused radially polarized beam (dotted blue). Particle size radius is (a) $r=10\text{ nm}$, (b) $r=25\text{ nm}$, (c) $r=50\text{ nm}$, (d) $r=70\text{ nm}$, and (e) $r=90\text{ nm}$	108
Fig. 4.6 Average radial intensity enhancement for an Au nanoparticle in glass ($nm = 1.52$) illuminated by a linearly polarized plane wave (black); tightly focused linearly polarized beam (dashed red); tightly focused radially polarized beam (dotted blue). Particle size radius is (a) $r=10\text{ nm}$, (b) $r=25\text{ nm}$, (c) $r=50\text{ nm}$, (d) $r=70\text{ nm}$, and (e) $r=90\text{ nm}$	109
Fig. 4.7 Average radial intensity enhancement for an Ag nanoparticle in air ($nm = 1.00$) illuminated by a linearly polarized plane wave (black); tightly focused linearly polarized beam (dashed red); tightly focused radially polarized beam (dotted blue) , and the particle radius is (a) $r=10\text{ nm}$, (b) $r=25\text{ nm}$, (c) $r=50\text{ nm}$, (d) $r=70\text{ nm}$, and (e) $r=90\text{ nm}$	110
Fig. 4.8 Average radial intensity enhancement for an Ag nanoparticle in glass ($nm = 1.52$) illuminated by a linearly polarized plane wave (black); tightly focused linearly polarized beam (dashed red); tightly focused radially polarized beam (dotted blue), and the particle radius is (a) $r=10\text{ nm}$, (b) $r=25\text{ nm}$, (c) $r=50\text{ nm}$, (d) $r=70\text{ nm}$, and (e) $r=90\text{ nm}$	110
Fig. 4.9 Average radial intensity enhancement for an incident tightly focused radially polarized beam interacting with an (a) uncoated Au (b) uncoated Ag, (c) Ag@Au, and (d) Au@Ag nanoparticle in different dielectric media air (black), BK7 (glass) ($\cdots$ red), and silicon ($- - -$ blue).	116
Fig. 4.10 Average radial intensity enhancement for an incident tightly focused radially polarized beam interacting with an Au@Ag nanoparticle of variable overall radius ranging from 20 nm to 100 nm and in different dielectric media (a) air (b) BK7 (glass), and (c) silicon.	119
Fig. 5.1 (a) Rays converging to focus. Shifted focal point due to (b) aberrated wave front, (c) refractive index mis-match.	126
Fig. 5.2 Wavefront of (a) spherical aberration, (b) defocus, (c) astigmatism, and (d) coma aberration.	127
Fig. 5.3 Electric field components of a tightly focused linearly polarized beam at the focal plane under spherical aberration ($As = 0.5\lambda$) (a) $Ex(x, y)$, (b) $Ey(x, y)$, and (c) $Ez(x, y)$. The results are normalized with the maximum value of the total absolute value of the electric field.	131
Fig. 5.4 Electric field components of a tightly focused linearly polarized beam at the focal plane under spherical aberration ($As = 1.0\lambda$) (a) $Ex(x, y)$, (b) $Ey(x, y)$, and (c) $Ez(x, y)$. The results are normalized with the maximum value of the total absolute value of the electric field.	131
Fig. 5.5 Scattering of a spherically aberrated tightly focused linearly polarized beam by a spherical nanoparticle.	132
Fig. 5.6 Average radial and tangential intensity enhancement for a spherically aberrated tightly focused linearly polarized beam having wavelength ranging from 300 nm to 900 nm scattering by an Au nanoparticle in air, respectively for (a), (b) half-integral $As = 0.5\lambda, 1.5\lambda, 2.5\lambda, 3.5\lambda$; and (c), (d) integral $As = 1.0\lambda, 2.0\lambda, 3.0\lambda, 4.0\lambda$	136
Fig. 5.7 Average radial and tangential intensity enhancement for a spherically aberrated tightly focused linearly polarized beam with wavelength range 300 nm to 900 nm and scattering by an Au nanoparticle in BK7 (glass) for (a), (b) half-integral $As = 0.5\lambda, 1.5\lambda, 2.5\lambda, 3.5\lambda$; and (c), (d) integral $As = 1.0\lambda, 2.0\lambda, 3.0\lambda, 4.0\lambda$	138

Fig. 5.8 Average radial and tangential intensity enhancement for a spherically aberrated tightly focused linearly polarized beam within wavelength range 300 nm to 900 nm and scattering by an Ag nanoparticle in air for (a), (b) half-integral $As = 0.5\lambda, 1.5\lambda, 2.5\lambda, 3.5\lambda$; and (c), (d) integral $As = 1.0\lambda, 2.0\lambda, 3.0\lambda, 4.0\lambda$.	140
Fig. 5.9 Average radial and tangential intensity enhancement for a spherically aberrated tightly focused linearly polarized beam having wavelength range 300 nm to 900 nm and scattering by an Ag nanoparticle in BK7 (glass) for (a), (b) half-integral $As = 0.5\lambda, 1.5\lambda, 2.5\lambda, 3.5\lambda$; and (c), (d) integral $As = 1.0\lambda, 2.0\lambda, 3.0\lambda, 4.0\lambda$.	142
Fig. 5.10 Variation in average radial and tangential intensity enhancement with As respectively, for an (a), (b) Au nanoparticle and (c), (d) Ag nanoparticle in two different media air, BK7 (glass).	145
Fig. 5.11 Relative strength of the expansion coefficients for a tightly focused linearly polarized beam ($\alpha = 60^\circ$) under a spherical aberration, $ An/A1 $ for (a) half-integral coefficients, and (b) integral coefficients.	146
Fig. 5.12 Average radial and tangential intensity enhancement factor with varying radius of an Au nanoparticle in (a), (b) air, and (c), (d) BK7 (glass) respectively, for $As = 0.0\lambda$ (without spherical aberration), and $As = 1.0\lambda$ (with spherical aberration).	147
Fig. 5.13 Average radial and tangential intensity enhancement factor with varying radius of an Ag nanoparticle in (a), (b) air, and (c), (d) BK7 (glass) respectively, for $As = 0.0\lambda$ (without spherical aberration), and $As = 1.0\lambda$ (with spherical aberration).	148
Fig. 5.14 Average radial and tangential intensity enhancement for an Au nanoparticle respectively, in (a), (b) air, and (c), (d) BK7 (glass) for a tightly focused linearly polarized beam with wavelength range 300 nm to 900 nm under three cases: (i) without aberration ($As = 0.0\lambda, Ad = 0.0\lambda$ (blue curve)) (ii) with spherical aberration ($As = 1.0\lambda, Ad = 0.0$ (··· red curve)), and (iii) with spherical aberration and defocusing ($As = 1.0\lambda, Ad = -As$ (--- green curve)).	149
Fig. 5.15 Average radial and tangential intensity enhancement for an Ag nanoparticle respectively, in (a), (b) air, and (c), (d) BK7 (glass) for a tightly focused linearly polarized beam with wavelength range 300 nm to 900 nm and under three cases: (i) without aberration ($As = 0.0\lambda, Ad = 0.0\lambda$ (blue curve)) (ii) with spherical aberration ($As = 1.0\lambda, Ad = 0.0$ (··· red curve)), and (iii) with spherical aberration and defocusing ($As = 1.0\lambda, Ad = -As$ (--- green curve)).	150
Fig. 5.16 For an Ag nanoparticle in BK7 (glass) medium the average (a) radial, and (b) tangential intensity enhancement varying with convergence angle for different values of spherical aberration As , at wavelength 418 nm. $As = 0.0\lambda$ (blue curve), $As = 0.5\lambda$ (green curve) $As = 1.0\lambda$ (red curve).	151

List of Tables

2.1 Sellmeier coefficients for BK7 (glass) and Silicon	63
2.2 Maximum Enhancement factor observed for Au and Ag nanoparticles under Plane Wave illumination	71
2.3 Maximum Enhancement factor for a varying Ag shell thickness of an Au@Ag core-shell NP (Au core radius $a = 6 \text{ nm}$) under a Plane Wave illumination	75
3.1 Maximum Enhancement factor observed for Au and Ag nanoparticles illuminated by tightly focused linearly polarized beam	92
3.2 Maximum Enhancement factor for a varying Ag shell thickness of an Au@Ag core-shell NP (Au core radius $a = 6 \text{ nm}$) under a tightly focused linearly polarized beam illumination	96
4.1 Maximum Enhancement factor observed for Au and Ag nanoparticles illuminated by the tightly focused radially polarized beam	107
4.2 Maximum Enhancement factor observed for Au nanoparticle under different conditions at wavelengths used in SERS	113
4.3 Maximum Enhancement factor observed for Ag nanoparticle under different conditions at wavelengths used in SERS	114
4.4 Maximum intensity enhancement for different nanoparticles under different illumination conditions	118
4.5 Maximum Enhancement factor for a varying Ag shell thickness of an Au@Ag core-shell nanoparticle (Au core radius $a = 6 \text{ nm}$) under a tightly focused radially polarized beam illumination	120
4.6 Maximum Enhancement factor observed for Au@Ag core-shell nanoparticle under different conditions	121
5.1 Intensity enhancement observed for an Au nanoparticle in air	137
5.2 Intensity enhancement for an Au nanoparticle in glass	139

5.3 Intensity enhancement for an Ag nanoparticle in air	141
5.4 Intensity enhancement for an Ag nanoparticle in glass	143