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- [1] **Pandey, D.**, Pandey, R.K., & Agarwal, R.P. (2023). Numerical approximation of fractional variational problems with several dependent variables using Jacobi poly-fractionomials. *Mathematics and Computers in Simulation*, 203, 28–43.

- [2] **Pandey, D.**, Kumar, K., & Pandey, R.K. (2023). Approximation schemes for a quadratic type generalized isoperimetric constraint fractional variational problems. *The Journal of Analysis*, 32, 191–218.

- [3] **Pandey, D.**, Pandey, P.K., & Pandey, R.K. (2024). Variational and Numerical Approximations for Higher-Order Fractional Sturm–Liouville Problems. *Communications on Applied Mathematics and Computation*, 1–21.

- [4] **Pandey, D.**, Pandey, R.K. Variational Approach for Solving Regular N-dimensional Fractional Sturm-Liouville Problems of Order Between $(0, 1]$. (*Communicated*).