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List of Publications

1. **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi, Relaxor ferroelectricity driven by 'A' and 'B' site off-centered displacements in cubic phase with $Pm\overline{3}m$ space group, Journal of Physics D: Applied Physics **54**, 365304 (2021).

2. **Digvijay Nath Dubey**, Gurvinderjit Singh, Akhilesh Kumar Singh, and Saurabh Tripathi, Role of Γ_4^- phonon mode in the enhancement of ferroelectric polarization in a perovskite-based eco-friendly functional material, EPL (Europhysics Letters) **140**, 26003 (2022).

3. Anuvrat Tripathi, **Digvijay Nath Dubey**, Harsh Kumar, and Saurabh Tripathi, Stabilising ferroelectricity in alkaline-earth-metal-based perovskites (ABO_3) *via* A-($Ca^{2+}/Sr^{2+}/Ba^{2+}$) and B-site (Ti^{4+}) cationic radius ratio (R_A/R_B), Journal of Applied Crystallography **55**, 1446 (2022).

4. Abhinav Kumar Singh, **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi, Tuning ferroelectricity by manipulating the global and local structure in a lead-free Sr doped $Ba(Ti_{1-x}Sn_x)O_3$ ceramics, EPL (Europhysics Letters) **130**, 36002 (2020).

5. Abhinav Kumar Singh, **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi, Unambiguous evidence of three coexisting ferroelectric phases in a lead-free $Li_xNa_{1-x}NbO_3$ system, Applied Physics Letters **116**, 232902 (2020).

Conferences/Schools

1. Gave an oral presentation on "Dielectrics 2022" organised by "IOP Institute of Physics" during 27/04/2022 to 29/04/2022.

   Paper title: Relaxor ferroelectricity in an average cubic ($Pm\overline{3}m$) phase of a lead-free smart material.

Authors: **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi.

2. Attended "Rigaku School for Practical Crystallography", organised by Rigaku Japan, January 10-21, 2022.

3. Poster presentation at "IUCr 2021- XXV General Assembly and Congress of the International Union of Crystallography", organised by Czech and Slovak Crystallographic Association, Ostricová 668/5, Stodulky, 155 00 Praha 5 Czech Republic, during 14-22 Aug, 2021.

   Paper Title: Ferroelectricity driven by 'A' and 'B' site off-centered displacements in cubic phase with $Pm\bar{3}m$ space group.

   Authors: **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi.

4. Gave an oral presentation at "4th International Conference on Science and Engineering of materials", organised by School of Basic Sciences and Research, Department of Physics, Sharda University, during July 19-22, 2021.

   Paper Title: Ferroelectricity driven by 'A' and 'B' site off-centered displacements in cubic phase with $Pm\bar{3}m$ space group.

   Authors: **Digvijay Nath Dubey**, Gurvinderjit Singh, and Saurabh Tripathi.

5. Attended "International Conference on Recent Advances in Material Science", organized By Department of Physics HNB Garhwal University, Srinagar Uttarakhand-India, during May 15-17, 2021.

6. Attended "International Conference on Functional Materials and Applied Physics", organised by Sardar Vallabhbhai National Institute of Technology, Surat, during May 14-15, 2021.