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*To*  
*My Beloved Parents*



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It is certified that the work contained in the thesis titled **Resilient Scheduling of Smart Buildings under False Data Injection Attack** by **Basant Kumar Sethi** has been carried out under my/our supervision and that this work has not been submitted elsewhere for a degree.

It is further certified that the student has fulfilled all the requirements of Comprehensive Examination, Candidacy and SOTA for the award of Ph.D. Degree.



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## DECLARATION

I, **Basant Kumar Sethi**, certify that the work embodied in this thesis is my own bonafide work and carried out by me under the supervision of **Prof. Devender Singh** and **Prof. Rakesh Kumar Misra** from July-2017 to June-2022, at the Department of Electrical Engineering, Indian Institute of Technology (BHU), Varanasi. The matter embodied in this thesis has not been submitted for the award of any other degree/diploma. I declare that I have faithfully acknowledged and given credits to the research workers wherever their works have been cited in my work in this thesis. I further declare that I have not willfully copied any other's work, paragraphs, text, data, results, etc., reported in journals, books, magazines, reports dissertations, theses, etc., or available at websites and have not included them in this thesis and have not cited as my own work.

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# Abstract

Modern Smart Home Energy Management Systems (SHEMSs) are inherently prone to cyber-attacks due to their high exposure to the Information and Communication Technology (ICT), thereby requirement of scheduling schemes resilient to cyber-attacks is important. Further, current scenario of SHEMS may result in increased charging and discharging cycles deteriorating the battery life. Therefore, demand scheduling formulations also need to cater the effect of battery degradation cost along with user comfort. The present work attempts to formulate a comprehensive scheduling problem in terms of energy cost minimization considering the battery degradation cost. Further, a cyber-attack resilient scheduling model is proposed in the present study. This work investigates the effect of demand scheduling on the life span of battery as well as the energy cost. Further, False Data Injection (FDI) attack has been modelled using machine learning techniques, and its effects on the scheduling has been incorporated in the objective function. Scenario tree based stochastic bill generation has also been formulated to develop an FDI attack resilient scheduling. Optimisation results of the study have established that the resulting formulation is robust against FDI attacks.

A game-theory based optimal and cyber-attack resilient energy scheduling in multiple smart buildings framework considering FDI attack has been proposed in this work. The proposed resilient scheduling is based on the consumers' past behaviour, and import and export power between the smart buildings and grids. An optimal resilient energy scheduling framework is designed considering Renewable Energy Sources (RESs), Combined Heat and Power (CHP) generators, Battery Storage Systems (BSSs), various Smart Home (SH) appliances and FDI attack. An iterative algorithm is used to solve a game-theory based Mixed Integer Quadratic Constrained Program (MIQCP) problem in General Algebraic Model System (GAMS) environment with a CPLEX solver. For identifying the FDI attack and making a resilient scheduling against possible attacks, the proposed technique

uses the difference between the actual and forecasted bills as well as maximum change in demand. The impacts of FDI attack which can be detrimental can be avoided, however, there may be a small difference between energy cost without considering attack and energy cost with considering resilient scheduling.

Further, the proposed resilient scheduling also been formulated for interconnected multiple smart buildings having power exchange capability among themselves. It is considered that each smart building is equipped with different types of Distributed Energy Resources (DERs), BSSs, CHP generators, Thermal Storage Systems (TSSs) and smart appliances.

Thus, in this work, a comprehensive optimal and robust scheduling is formulated to mitigate the effects of FDI attacks. The proposed method uses the information of anomaly between the actual and forecasted bills for detecting the cyber attack and making a resilient scheduling against possible attacks.

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# Nomenclature

## Abbreviations

|      |                                   |
|------|-----------------------------------|
| 2PE  | Two-Point Estimation method       |
| AC   | Air Conditioner                   |
| BEMS | Building Energy Management System |
| BS   | Battery Storage                   |
| BSS  | Battery Storage System            |
| CHP  | Combined Heat and Power           |
| CVaR | Conditional Value at Risk         |
| DERs | Distributed Energy Resources      |
| SLs  | Schedulable Loads                 |
| DOD  | Depth of Discharge                |
| DR   | Demand Response                   |
| DSM  | Demand-Side Management            |
| EMU  | Energy Management Unit            |
| EV   | Electric Vehicle                  |
| EWH  | Electric Water Heater             |
| FDI  | False Data Injection              |

|        |   |
|--------|---|
| UNLs   | Unschedulable and Noninterruptible Loads      |
| GA     | Genetic Algorithm                             |
| GPR    | Gaussian Process Regression                   |
| GWO    | Grey wolf optimizer                           |
| HAN    | Home Area Network                             |
| HEMS   | Home Energy Management System                 |
| ICT    | Information and Communication Technology      |
| IT     | Information Technology                        |
| LMU    | Load Management Unit                          |
| LP     | Linear Programming                            |
| MILP   | Mixed-Integer Linear Programming              |
| MINLP  | Mixed-Integer Nonlinear Programming           |
| MIQCP  | Mixed-Integer Quadratic Programming           |
| MSB    | Multi Smart Building                          |
| MSBEMS | Multi Smart Building Energy Management System |
| MULP   | Multiple-Users and Load Priority              |
| PAR    | Peak-to-Average Ratio                         |
| MDL    | Maximum Demand Limit                          |
| PE     | Point Estimation                              |
| PEL    | Power Export Limit                            |
| PHEV   | Plug-in Hybrid Electric Vehicle               |
| PR     | Power Ratio                                   |

|       |                                     |
|-------|-------------------------------------|
| PV    | Photovoltaic cell                   |
| RE    | Renewable Energy                    |
| RES   | Renewable Energy Source             |
| RMSE  | Root Mean Square Error              |
| RTP   | Real Time Pricing                   |
| SB    | Smart Building                      |
| SH    | Smart Home                          |
| SHEMS | Smart Home Energy Management System |
| SOC   | State of Charge                     |
| TC    | Thermal Capacity                    |
| TDLs  | Temperature Dependent Loads         |
| TOU   | Time of Use                         |
| TSS   | Thermal Storage System              |
| TSOC  | State of Charge of TSS              |
| UN    | Utility Network                     |
| PRL   | Part Load Ratio                     |
| SM    | smart meter                         |

## List of sets, parameters and variables

|           |                                 |
|-----------|---------------------------------|
| $a_s$     | number of SLs                   |
| $a_u$     | number of UNLs                  |
| $a_{td}$  | number of TDLs                  |
| $t$       | index of time                   |
| $b$       | index of buildings              |
| $h$       | index of smart home             |
| $w$       | index of scenario               |
| $P^s$     | solar PV power in $kW$          |
| $DF$      | derating factor                 |
| $P_{STC}$ | nominal PV array power          |
| $G_{STC}$ | solar radiance at STC           |
| $G_A$     | global solar radiation          |
| $T_{STC}$ | temperature under STC           |
| $C_T$     | PV temperature co-efficient     |
| $T_C$     | solar PV cell temperature       |
| $G$       | global solar radiation          |
| $BC$      | battery capacity                |
| $f$       | false injected data             |
| $h$       | actual smart meter data         |
| $y$       | smart meter output after attack |
| $\mu$     | mean                            |

|                 |                                      |
|-----------------|--------------------------------------|
| $\sigma$        | standard deviation                   |
| $T_a$           | ambient temperature                  |
| $NT$            | normal operating cell temperature    |
| $P^w$           | wind power in $kW$                   |
| $C_P$           | power co-efficient                   |
| $V$             | wind speed in $meter/sec$            |
| $A$             | swept area in $m^2$                  |
| $\rho$          | air density                          |
| $\sigma$        | self discharging of battery          |
| $P^{ch}$        | charging power of battery            |
| $P_{max}^{ch}$  | maximum charging power of battery    |
| $P^{dis}$       | discharging power of battery         |
| $P_{max}^{dis}$ | maximum discharging power of battery |
| $\eta^{ch}$     | battery charging efficiency          |
| $\eta^{dis}$    | battery discharging efficiency       |
| $\Delta t$      | time interval                        |
| $P_c^{chp}$     | CHP rated capacity                   |
| $P^{chp}$       | CHP output power                     |
| $H^{chp}$       | CHP heat output                      |
| $P_{TE}$        | CHP heat to electrical power ratio   |
| $T^{in}$        | internal temperature of refrigerator |
| $\epsilon$      | inertia constant for refrigerator    |

|                  |   |
|------------------|---|
| $\epsilon_{air}$ | factor of inertia of air for AC                     |
| $\eta_{rf}$      | efficiency of refrigerator                          |
| $K_{rf}$         | insulation constant of refrigerator                 |
| $P_{rf}$         | power consumption of refrigerator                   |
| $P_{rrf}$        | rated power of refrigerator                         |
| $S_{rf}$         | ON/OFF status of refrigerator                       |
| $T_r$            | room temperature for AC                             |
| $P_{rac}$        | rated power of AC                                   |
| $K_{air}$        | thermal conductivity of AC                          |
| $\eta_{ac}$      | efficiency of AC                                    |
| $S_{ac}$         | binary status of AC                                 |
| $P_{ac}$         | power consumption of AC                             |
| $T_r^{min}$      | minimum room temperature                            |
| $T_r^{max}$      | maximum room temperature                            |
| $P_{SL}$         | power consumption by SL                             |
| $S_{a_s}$        | binary status of $a_s$ appliance                    |
| $P_{a_s}$        | rated power of $a_s$ appliance                      |
| $C_{dis}$        | degradation cost due discharging cycle              |
| $C_{in}$         | initial investment cost of battery                  |
| $n_{std}$        | permissible number of charging or discharging cycle |
| $D$              | average DOD of battery                              |
| $C_{DOD}$        | battery degradation cost due to DOD                 |

|                 |   |
|-----------------|---|
| $C_{cyc}$       | battery degradation cost                              |
| $B^p$           | predicted bill  |
| $\pi$           | probability   |
| $E$             | net energy of smart home                              |
| $C$             | electricity cost                                      |
| $P_{UNLs}$      | power consumption of UNLs                             |
| $P_{TDLs}$      | power consumption of TDLs                             |
| $P^r$           | renewable power generation                            |
| $d_{a_s}$       | time duration of appliance $a_s$ to complete the task |
| $tin_{a_s}$     | starting time of appliance $a_s$                      |
| $tout_{a_s}$    | ending time of appliance $a_s$                        |
| $P_{mdl}$       | maximum demand limit                                  |
| $T^{min}$       | minimum temperature                                   |
| $T^{max}$       | maximum temperature                                   |
| $SOC^{min}$     | minimum SOC   |
| $SOC^{max}$     | maximum SOC   |
| $B$             | actual bill   |
| $\gamma$        | attacked price  |
| $\lambda_g$     | natural gas price                                     |
| $\lambda_x$     | power export price                                    |
| $\lambda$       | reference/forecasted price                            |
| $\lambda_{bmc}$ | battery maintenance cost                              |

|                 |   |
|-----------------|---|
| $P^R$           | forecasted demand                               |
| $\tau$          | tolerance                                       |
| $P^{gimp}$      | grid import power                               |
| $P^{gexp}$      | grid export power                               |
| $P^{gex}$       | grid exchange power                             |
| $P_{bim}$       | building import power                           |
| $P_{bex}$       | building export power                           |
| $P_{a_i}$       | total power consumption of $a_i^{th}$ appliance |
| $P_{rated,a_i}$ | rated power of $a_i^{th}$ appliance             |
| $P_b$           | demand of $b^{th}$ smart building               |
| $\alpha_b$      | binary variable of grid                         |
| $\alpha_1$      | binary variable of battery storage system       |
| $P^{disT}$      | discharging power of TSS                        |
| $P^{chT}$       | charging power of TSS                           |
| $\eta^{disT}$   | discharging efficiency of TSS                   |
| $\eta^{chT}$    | charging efficiency of TSS                      |
| $\alpha_2$      | binary variable of thermal storage system       |
| $SOC^T$         | SOC of TSS                                      |
| $SOC^T$         | SOC of TSS                                      |
| $H_h$           | total heat demand of $h^{th}$ SH                |
| $H^{disT}$      | discharging heat of TSS                         |
| $H^{chT}$       | charging heat of TSS                            |