

Morphology Evolution and Kinetics of Block Copolymer Systems



Thesis submitted in fulfillment
for the Award of

Doctor of Philosophy
in
Physics

by

Avinash Chauhan

to the

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August 2024

To my parents,
Shrimati Shakuntala Chauhan,
Shri Sury Nath Chauhan

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