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List of Publications

- [1] **V. Agrawal** and T. Som, *Fractal dimension of α -fractal function on the Sierpiński Gasket*, Eur. Phys. J. Spec. Top. 230, 3781-3787, 2021.
- [2] **V. Agrawal**, T. Som, S. Verma, *A note on stability and fractal dimension of bivariate α -fractal functions*, Numer Algor, 2023.
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