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# Appendix A

## Benchmark points for the Yukawa couplings of $\mathcal{L}_N \times \mathcal{L}_M$ flavour symmetry

We perform a  $\chi^2$  fit to the quark and charged-lepton masses, along with the quark mixing parameters, by defining,

$$\begin{aligned} \chi^2 = & \frac{(m_q - m_q^{\text{model}})^2}{\sigma_{m_q}^2} + \frac{(m_\ell - m_\ell^{\text{model}})^2}{\sigma_{m_\ell}^2} + \frac{(\sin \theta_{ij} - \sin \theta_{ij}^{\text{model}})^2}{\sigma_{\sin \theta_{ij}}^2} \\ & + \frac{(\sin 2\beta - \sin 2\beta^{\text{model}})^2}{\sigma_{\sin 2\beta}^2} + \frac{(\alpha - \alpha^{\text{model}})^2}{(\sigma_\alpha)^2} + \frac{(\gamma - \gamma^{\text{model}})^2}{(\sigma_\gamma)^2}, \end{aligned} \quad (\text{A.1})$$

where  $q = \{u, d, c, s, t, b\}$ ,  $\ell = \{e, \mu, \tau\}$ , and  $i, j = 1, 2, 3$ . The CKM matrix phases in the standard parametrization are given by,

$$\begin{aligned} \beta^{\text{model}} &= \arg \left( -\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*} \right), \\ \alpha^{\text{model}} &= \arg \left( -\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*} \right), \\ \gamma^{\text{model}} &= \arg \left( -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right). \end{aligned} \quad (\text{A.2})$$

To reproduce the fermion masses, we use the following values of the quark and charged-lepton masses at 1TeV [294],

$$\begin{aligned} \{m_t, m_c, m_u\} &\simeq \{150.7 \pm 3.4, 0.532_{-0.073}^{+0.074}, (1.10_{-0.37}^{+0.43}) \times 10^{-3}\} \text{ GeV}, \\ \{m_b, m_s, m_d\} &\simeq \{2.43 \pm 0.08, 4.7_{-1.3}^{+1.4} \times 10^{-2}, 2.50_{-1.03}^{+1.08} \times 10^{-3}\} \text{ GeV}, \\ \{m_\tau, m_\mu, m_e\} &\simeq \{1.78 \pm 0.2, 0.105_{-9.3 \times 10^{-9}}^{+9.4 \times 10^{-9}}, 4.96 \pm 0.00000043 \times 10^{-4}\} \text{ GeV}. \end{aligned} \quad (\text{A.3})$$

The magnitudes and phases of the CKM mixing elements are [152],

$$\begin{aligned} |V_{ud}| &= 0.97370 \pm 0.00014, |V_{cb}| = 0.0410 \pm 0.0014, |V_{ub}| = 0.00382 \pm 0.00024, \\ \sin 2\beta &= 0.699 \pm 0.017, \alpha = (84.9_{-4.5}^{+5.1})^\circ, \gamma = (72.1_{-4.5}^{+4.1})^\circ, \delta = 1.196_{-0.043}^{+0.045} \end{aligned} \quad (\text{A.4})$$

## The $\mathcal{L}_2 \times \mathcal{L}_5$ model

The dimensionless coefficients  $y_{ij}^{u,d,\ell,\nu} = |y_{ij}^{u,d,\ell,\nu}| e^{i\phi_{ij}^{q,\ell,\nu}}$  are scanned with  $|y_{ij}^{u,d,\ell,\nu}| \in [0.1, 4\pi]$  and  $\phi_{ij}^{q,\ell,\nu} \in [0, 2\pi]$ . The fit results are,

$$\begin{aligned} Y_u &= \begin{pmatrix} -1.68 - 3.37i & -0.09 + 0.03i & -0.1 - 0.02i \\ 1.53 + 4.95i & -0.57 + 0.55i & 0.48 + 0.002i \\ 0.76 + 0.18i & -1.04 + 0.46i & 0.58 - 0.65i \end{pmatrix}, \\ Y_d &= \begin{pmatrix} -4.15 + 3.58i & 2.20 - 0.89i & 2.62 - 4.20i \\ -0.33 - 0.36i & 0.07 - 0.075i & 0.17 + 0.47i \\ -0.24 - 0.07i & -0.06 - 0.084i & -0.07 - 0.12i \end{pmatrix}, \end{aligned}$$

$$Y_l = \begin{pmatrix} -0.07 - 0.06i & 0.099 - 0.004i & 0.45 - 0.32i \\ -0.14 - 0.09i & 0.08 - 0.06i & -0.63 + 0.24i \\ -0.04 + 0.09i & -0.09 + 0.06i & 0.10 - 0.0003i \end{pmatrix}.$$

with  $\varepsilon = 0.1$ ,  $\delta = 1.196$ , and  $\chi_{min}^2 = 3.16$ .

### The $\mathcal{L}_2 \times \mathcal{L}_9$ model

The dimensionless coefficients  $y_{ij}^{u,d,\ell,v} = |y_{ij}^{u,d,\ell,v}| e^{i\phi_{ij}^{q,\ell,v}}$  are scanned with  $|y_{ij}^{u,d,\ell,v}| \in [0.9, 2\pi]$  and  $\phi_{ij}^{q,\ell,v} \in [0, 2\pi]$ . The fit results are,

$$Y_u = \begin{pmatrix} 1 & 0.87 - 0.49i & -0.23 + 0.97i \\ -0.9 + 1.05i & -0.7 - 0.72i & 1 \\ 0.94 - 0.33i & 0.55 + 0.84i & 0.9 \end{pmatrix},$$

$$Y_d = \begin{pmatrix} 0.99 - 0.09i & 3.24 - 1.05i & 1 \\ 0.99 - 0.10i & 0.92 + 0.39i & 0.9 \\ 1 & 1 & -1.04 + 0.54i \end{pmatrix},$$

$$Y_l = \begin{pmatrix} 0.9 & 0.9 & 1.5 \\ 0.9 & 1.5 & 1.5 \\ 1.5 & 1.5 & 0.9 \end{pmatrix}.$$

with  $\varepsilon = 0.23$ ,  $\delta = 1.196$ , and  $\chi_{min}^2 = 5.91$ .

**The  $\mathcal{L}_2 \times \mathcal{L}_{11}$  model**

The dimensionless coefficients  $y_{ij}^{u,d,\ell,\nu} = |y_{ij}^{u,d,\ell,\nu}| e^{i\phi_{ij}^{q,\ell,\nu}}$  are scanned with  $|y_{ij}^{u,d,\ell,\nu}| \in [0.7, 2\pi]$  and  $\phi_{ij}^{q,\ell,\nu} \in [0, 2\pi]$ . The fit results are,

$$Y_u = \begin{pmatrix} 2.19 - 0.18i & 1.40 - 0.09i & 0.70 - 0.002i \\ 2.12 + 0.02i & -1.02 + 2.12i & 4.45 - 1.01i \\ 0.33 - 0.71i & 0.92 + 0.42i & 0.82 - 0.26i \end{pmatrix},$$
$$Y_d = \begin{pmatrix} 0.40 + 0.59i & 3.61 - 0.16i & 3.34 - 4.06i \\ 1.02 + 0.01i & -0.36 + 1.18i & 1.29 + 0.36i \\ -0.77 + 0.33i & 0.82 + 0.02i & -0.51 + 0.48i \end{pmatrix}$$
$$Y_l = \begin{pmatrix} -0.73 + 0.001i & -0.58 + 0.53i & 0.001 + 1.29i \\ 6.24 + 0.37i & 3.48 - 2.44i & 1.71 + 1.7 \times 10^{-5}i \\ 0.24 - 1.16i & -0.36 - 0.61i & -0.60 + 0.35i \end{pmatrix}$$

with  $\varepsilon = 0.28$ ,  $\delta = 1.196$ , and  $\chi_{min}^2 = 11.82$ .

## The $\mathcal{L}_8 \times \mathcal{L}_{22}$ model

The dimensionless coefficients  $y_{ij}^{u,d,\ell,\nu} = |y_{ij}^{u,d,\ell,\nu}| e^{i\phi_{ij}^{q,\ell,\nu}}$  are scanned with  $|y_{ij}^{u,d,\ell,\nu}| \in [0.9, 2]$  and  $\phi_{ij}^{q,\ell,\nu} \in [0, 2\pi]$ . The fit results are,

$$Y_u = \begin{pmatrix} 0.12 + 1.44i & -0.38 - 0.82i & 0.989 + 0.004i \\ -1.27 - 1.38i & -0.56 + 0.82i & -1.22 - 0.24i \\ -1.12 - 0.25i & -1.12 - 0.43i & -2.70 - 2.61i \end{pmatrix},$$

$$Y_d = \begin{pmatrix} -1.36 + 0.39i & 0.31 - 1.28i & 0.71 + 0.61i \\ -1.05 + 0.27i & -0.44 + 0.85i & 0.47 - 0.79i \\ -1.11 - 0.37i & -0.81 + 0.42i & 0.80 + 0.82i \end{pmatrix}$$

$$Y_l = \begin{pmatrix} -1.40 - 0.21i & 1.14 - 0.004i & -0.78 + 0.45i \\ -0.88 + 0.16i & -0.54 + 0.78i & -1.16 + 0.11i \\ 0.85 + 0.34i & 0.899 + 0.003i & 0.899 - 0.003i \end{pmatrix}$$

with  $\varepsilon = 0.23$ ,  $\delta = 1.196$ , and  $\chi_{min}^2 = 1.62$ .

## The SM background

Production mode	Channel	SM Backgrounds
Inclusive production	jet-jet	$pp \rightarrow jj$
	$\ell^+\ell^- (\ell = e, \mu, \tau)$	$pp \rightarrow \ell^+\ell^-$
	$\mu e$	$pp \rightarrow t\bar{t}, pp \rightarrow VV (V = W^+, W^-, Z),$ $pp \rightarrow \ell^+\ell^-, pp \rightarrow tWb$
	$\mu\tau, e\tau$	$pp \rightarrow$ multijets, $pp \rightarrow W+$ jets , $pp \rightarrow t\bar{t}, pp \rightarrow VV (V = W^+, W^-, Z),$ $pp \rightarrow \ell^+\ell^-, pp \rightarrow tWb$
	$b\bar{b}$	$pp \rightarrow b\bar{b}$
	$\gamma\gamma$	$pp \rightarrow \gamma\gamma$
	$t\bar{t}$	$pp \rightarrow t\bar{t}$
Associative production	$t\bar{t}a \rightarrow t\bar{t}\bar{t}$	$pp \rightarrow t\bar{t}\bar{t}$
	$abb \rightarrow \tau\tau bb$	$pp \rightarrow \tau\tau bb$
	$ab \rightarrow \tau\tau b$	$pp \rightarrow$ multijets, $pp \rightarrow W+$ jets, $pp \rightarrow t\bar{t}$ $pp \rightarrow \ell^+\ell^-, pp \rightarrow tWb, pp \rightarrow VV$
Di-flavon production	$aa \rightarrow b\bar{b}\ell\ell (\ell = \mu, \tau)$	$pp \rightarrow b\bar{b}\ell\ell$
	$aa \rightarrow bbbb$	$pp \rightarrow bbbb$

Table A.1 SM Backgrounds for the flavon production through various channels.

## Benchmark points for the Yukawa couplings of the SHVM

We reproduce the fermion masses using the values of the fermion masses at 1TeV, given in equation A.3. For this, we conduct a  $\chi^2$  fit to the masses of quarks and charged leptons, as well as the parameters describing quark mixing, in the similar way as done in section A.

The dimensionless coefficients  $y_{ij}^{u,d,\ell,\nu} = |y_{ij}^{u,d,\ell,\nu}| e^{i\phi_{ij}^{q,\ell,\nu}}$  are scanned with  $|y_{ij}^{u,d,\ell,\nu}| \in [0.1, 4\pi]$  and  $\phi_{ij}^{q,\ell,\nu} \in [0, 2\pi]$ . The fit results are,

$$y_{ij}^u = \begin{pmatrix} 1.002 + 1.730i & 0 & 0.580 + 1.944i \\ 0 & -0.892 + 0.450i & -0.974 - 0.140i \\ 0 & -0.320 + 1.597i & 0.999 - 0.016i \end{pmatrix},$$

$$y_{ij}^d = \begin{pmatrix} -1.071 + 0.086i & -0.094 + 0.0897i & 0.080 - 0.086i \\ 0.554 - 0.744i & 1.212 - 0.209i & 1.211 + 0.238i \\ 0.305 + 1.978i & -1.142 + 0.139i & -1.175 - 0.019i \end{pmatrix},$$

We obtain  $\delta_{\text{CP}}^q \approx 1.144$  for Dirac CP phase.

$$y_{ij}^\ell = \begin{pmatrix} 0.902 - 0.093i & 0.523 - 0.887i & 0.356 - 1.041i \\ 0 & 0.295 + 2.341i & 0.422 + 1.016i \\ 0 & 0 & 3.173 + 5.834 \times 10^{-9}i \end{pmatrix},$$

The neutrino couplings for normal mass ordering are,

$$y_{ij}^\nu = \begin{pmatrix} 0.6 - 0.88i & 0.87 - 0.41i & 1.5 - 0.00004i \\ 0 & 0.96 + 0.12i & -0.52 - 1.41i \\ 0 & -1.43 + 0.28i & 1.5 + 0.00004i \end{pmatrix},$$

and the leptonic Dirac CP phase turns out to be  $\delta_{\text{CP}}^\ell \approx 3.14$ .

## Bi-unitary transformation matrices in SHVM

$$U_u = \begin{pmatrix} -0.973 - 0.233i & -4.156 \times 10^{-5} - 9.950 \times 10^{-6}i & 5.064 \times 10^{-8} + 1.213 \times 10^{-8}i \\ 9.075 \times 10^{-6} + 4.175 \times 10^{-5}i & -0.212 - 0.977i & -0.002 - 0.010i \\ 4.858 \times 10^{-7} + 0.000i & -0.010 + 0.000i & 1.000 + 0.000i \end{pmatrix}$$

$$V_u = \begin{pmatrix} 0.270 + 0.963i & -1.516 \times 10^{-2} - 1.394 \times 10^{-2}i & 1.929 \times 10^{-3} + 6.868 \times 10^{-3}i \\ 1.271 \times 10^{-2} + 1.620 \times 10^{-2}i & 0.939 + 0.344i & -2.806 \times 10^{-4} - 2.064 \times 10^{-5}i \\ -7.129 \times 10^{-3} + 0.000i & 3.955 \times 10^{-4} + 0.000i & 1.000 + 0.000i \end{pmatrix}$$

$$U_d = \begin{pmatrix} -8.408 \times 10^{-2} - 8.859 \times 10^{-2}i & -2.487 \times 10^{-1} + 5.717 \times 10^{-1}i & 1.301 \times 10^{-1} - 7.613 \times 10^{-1}i \\ -6.040 \times 10^{-1} - 2.561 \times 10^{-1}i & -5.112 \times 10^{-1} - 3.329 \times 10^{-1}i & -4.401 \times 10^{-1} - 6.160 \times 10^{-2}i \\ 7.449 \times 10^{-1} + 0.000i & -4.891 \times 10^{-1} + 0.000i & -4.540 \times 10^{-1} + 0.000i \end{pmatrix}$$

$$V_d = \begin{pmatrix} -4.824 \times 10^{-1} + 8.635 \times 10^{-1}i & 1.107 \times 10^{-1} - 9.716 \times 10^{-2}i & -2.149 \times 10^{-4} + 3.632 \times 10^{-3}i \\ -1.471 \times 10^{-1} - 2.873 \times 10^{-3}i & -9.248 \times 10^{-1} - 3.493 \times 10^{-1}i & -3.088 \times 10^{-2} - 1.125 \times 10^{-2}i \\ -7.820 \times 10^{-3} + 0.000i & -3.213 \times 10^{-2} + 0.000i & 9.995 \times 10^{-1} + 0.000i \end{pmatrix}$$

$$U_\ell = \begin{pmatrix} -1.457 \times 10^{-1} - 9.893 \times 10^{-1}i & -1.572 \times 10^{-4} + 4.160 \times 10^{-4}i & 3.416 \times 10^{-6} - 7.407 \times 10^{-6}i \\ -3.177 \times 10^{-4} + 3.113 \times 10^{-4}i & -9.642 \times 10^{-1} + 2.645 \times 10^{-1}i & 1.989 \times 10^{-2} - 5.455 \times 10^{-3}i \\ 1.188 \times 10^{-6} + 0.000i & 2.062 \times 10^{-2} + 0.000i & 9.998 \times 10^{-1} + 0.000i \end{pmatrix}$$

$$V_\ell = \begin{pmatrix} -2.455 \times 10^{-1} - 9.644 \times 10^{-1}i & -2.395 \times 10^{-2} + 9.067 \times 10^{-2}i & 9.415 \times 10^{-3} - 2.756 \times 10^{-2}i \\ -7.731 \times 10^{-2} - 6.040 \times 10^{-2}i & -3.598 \times 10^{-1} - 8.677 \times 10^{-1}i & 1.260 \times 10^{-1} + 3.034 \times 10^{-1}i \\ 4.024 \times 10^{-3} + 0.000i & 3.298 \times 10^{-1} + 0.000i & 9.440 \times 10^{-1} + 0.000i \end{pmatrix}$$

## Scalar mass matrix diagonalization in SHVM

$$m_s^2 = \lambda_\chi \Lambda^2 \begin{pmatrix} 16\varepsilon_7^2 & 8\varepsilon_1\varepsilon_7 & 8\varepsilon_4\varepsilon_7 & 8\varepsilon_5\varepsilon_7 & 8\varepsilon_2\varepsilon_7 & 8\varepsilon_6\varepsilon_7 & 8\varepsilon_3\varepsilon_7 \\ 8\varepsilon_1\varepsilon_7 & 16\varepsilon_1^2 & 8\varepsilon_1\varepsilon_4 & 8\varepsilon_1\varepsilon_5 & 8\varepsilon_1\varepsilon_2 & 8\varepsilon_1\varepsilon_6 & 8\varepsilon_1\varepsilon_3 \\ 8\varepsilon_4\varepsilon_7 & 8\varepsilon_1\varepsilon_4 & 16\varepsilon_4^2 & 8\varepsilon_4\varepsilon_5 & 8\varepsilon_2\varepsilon_4 & 8\varepsilon_4\varepsilon_6 & 8\varepsilon_3\varepsilon_4 \\ 8\varepsilon_5\varepsilon_7 & 8\varepsilon_1\varepsilon_5 & 8\varepsilon_4\varepsilon_5 & 16\varepsilon_5^2 & 8\varepsilon_2\varepsilon_5 & 8\varepsilon_5\varepsilon_6 & 8\varepsilon_3\varepsilon_5 \\ 8\varepsilon_2\varepsilon_7 & 8\varepsilon_1\varepsilon_2 & 8\varepsilon_2\varepsilon_4 & 8\varepsilon_2\varepsilon_5 & 16\varepsilon_2^2 & 8\varepsilon_2\varepsilon_6 & 8\varepsilon_2\varepsilon_3 \\ 8\varepsilon_6\varepsilon_7 & 8\varepsilon_1\varepsilon_6 & 8\varepsilon_4\varepsilon_6 & 8\varepsilon_5\varepsilon_6 & 8\varepsilon_2\varepsilon_6 & 16\varepsilon_6^2 & 8\varepsilon_3\varepsilon_6 \\ 8\varepsilon_3\varepsilon_7 & 8\varepsilon_1\varepsilon_3 & 8\varepsilon_3\varepsilon_4 & 8\varepsilon_3\varepsilon_5 & 8\varepsilon_2\varepsilon_3 & 8\varepsilon_3\varepsilon_6 & 16\varepsilon_3^2 \end{pmatrix},$$

$$U = \begin{pmatrix} 1 & -3.24 \times 10^{-4} & -1.94 \times 10^{-6} & -5.34 \times 10^{-7} & -4.88 \times 10^{-8} & 4.69 \times 10^{-8} & 4.14 \times 10^{-10} \\ -3.24 \times 10^{-4} & -0.999 & -8.56 \times 10^{-3} & -2.35 \times 10^{-3} & -2.15 \times 10^{-4} & 2.06 \times 10^{-4} & 1.82 \times 10^{-6} \\ -1.68 \times 10^{-6} & 8.66 \times 10^{-3} & -0.999 & -4.73 \times 10^{-2} & -4.18 \times 10^{-3} & 3.98 \times 10^{-3} & 3.52 \times 10^{-4} \\ -3.79 \times 10^{-7} & 1.95 \times 10^{-2} & 4.75 \times 10^{-2} & -0.998 & -1.85 \times 10^{-2} & 1.77 \times 10^{-2} & 1.56 \times 10^{-4} \\ -3.37 \times 10^{-8} & 1.73 \times 10^{-4} & 3.95 \times 10^{-3} & 2.25 \times 10^{-2} & -0.968 & 2.49 \times 10^{-1} & 1.76 \times 10^{-3} \\ -1.89 \times 10^{-8} & 9.75 \times 10^{-5} & 2.23 \times 10^{-3} & 1.26 \times 10^{-2} & 2.499 \times 10^{-1} & 0.97 & 3.12 \times 10^{-3} \\ -1.18 \times 10^{-10} & 6.08 \times 10^{-7} & 1.39 \times 10^{-5} & 7.84 \times 10^{-4} & 9.27 \times 10^{-4} & -3.46 \times 10^{-3} & 0.999 \end{pmatrix}$$

$$M_{dia}^2 = \lambda_\chi \Lambda^2 \text{dia} \left( 4.71 \times 10^{-18}, 9.33 \times 10^{-11}, 3.56 \times 10^{-8}, 7.30 \times 10^{-7}, 9.45 \times 10^{-5}, 3.67 \times 10^{-4}, 12.01 \right).$$