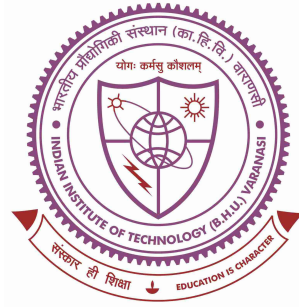


Using gravitational lensing to probe distribution of neutral hydrogen in the post-reionization Universe



THESIS SUBMITTED
FOR THE AWARD OF
DOCTOR OF PHILOSOPHY
in
PHYSICS
by
URVASHI

DEPARTMENT OF PHYSICS
INDIAN INSTITUTE OF TECHNOLOGY
BANARAS HINDU UNIVERSITY
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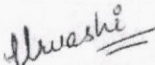
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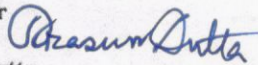
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**In the honour
of
My Parents**

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