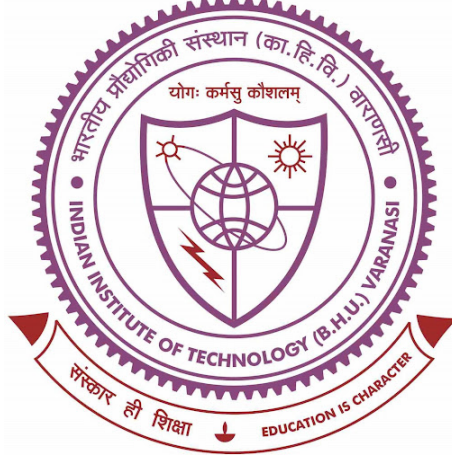

On the Weyl transform



Thesis submitted in partial fulfillment

for the award of the degree

DOCTOR OF PHILOSOPHY

by

Mansi Mishra

DEPARTMENT OF MATHEMATICAL SCIENCES

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December 2024



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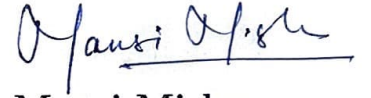
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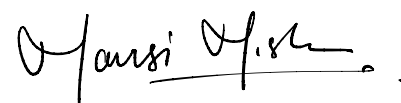
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Dedicated
to
my grandfather, Mr. S. C. Mishra

ACKNOWLEDGEMENTS

First and foremost, I would like to express my deepest gratitude to my advisor, Prof. M. K. Vemuri. Your unwavering support, guidance, and boundless patience have been the cornerstones of my research journey. Your mentorship has not only shaped this thesis but also profoundly influenced my growth as a scholar. I am immensely grateful for your encouragement, expertise, and the countless hours you have invested in my development.

I would like to thank my RPEC members, Prof. T. Som, Prof. R. K. Mishra, and Dr. Sheela Verma, for their constant support and their insightful comments, which encouraged me to view my research from various perspectives. I extend my sincere gratitude to Prof. S. K. Pandey, Head of the Department of Mathematical Sciences, and Dr. Anuradha Banerjee, Convener of the DPGC of the Department of Mathematical Sciences, IIT (BHU), for their unwavering support during my research. I extend my profound gratitude to all faculty members, research scholars, and non-teaching staff of my department. I wish to express my gratitude for the resources offered by my department and institute to facilitate my research activities. I would also like to acknowledge the financial assistance given to me by the institute in the form of fellowships and financial allowances for attending conferences.

I was fortunate enough to pursue my masters from IIT Kanpur, one of the best institutes in India. IITK has given me countless opportunities and memories. I am very thankful to all the faculty members of the Department of Mathematics, IITK. I would like to thank all my friends and colleagues from IITK for making those two years the best time of my life. Words cannot express my love for that

beautiful campus. I learned a lot about life and mathematics while I was pursuing the bachelors degree from Sri Venkateswara College, Delhi University. I am deeply thankful to my inspiring teachers and wonderful friends at DU, who made my time there truly unforgettable.

I am blessed to have a very supportive family. I owe my sincere thanks to my parents, Mrs. Mamta Mishra and Mr. S. M. Mishra. Your unconditional love, sacrifices, and encouragement have been a constant source of strength and motivation throughout my life. Your belief in my abilities has been a driving force behind every step I have taken in my academic journey. To my amazing brother, Mr. Mohit Mishra, thank you for being a constant source of inspiration and strength. You have been an incredible role model, and I have always aspired to emulate your drive and dedication to your career. Your unwavering commitment has inspired me to strive for similar excellence in my own pursuits.

I dedicate this achievement to the loving memory of my grandfather, Mr. S. C. Mishra, whose unwavering faith in my abilities inspired me to pursue academic excellence. His presence is deeply missed, but his legacy continues to motivate me. I acknowledge with sincere appreciation the supportive presence of my grandmother, Mrs. Rajkishori Devi, throughout my academic and personal journey. To my family members, Mrs. Ekta Tiwari, Mrs. Mrinalini Tiwari, Mr. Nishant Nayan, and Mr. S. K. Tiwari, your understanding, support, and the countless moments of encouragement have been invaluable. I am grateful to my amazing cousins, Sanidhya, Satwik, Ananya, and Agastya, for adding the much needed cheer to this thesis writing journey and to my life in general.

We all faced a very difficult time in 2020, when the COVID pandemic wreaked havoc on the world. Like many others, I experienced an overwhelming sense of anxiety and demotivation; however, I was fortunate to have the support of numerous individuals during that challenging period. I want to thank my uncle Dr. Awanish Kumar, my

aunt Dr. Anisha George, my advisor, and my mother for providing me the comfort and the much needed motivation in that difficult time.

I would like to thank my chamber-mates, Ms. Ankita Sharma, Mr. Manish Chaurasia, Ms. Pooja Rani, and Mr. Promod Sharma for their support throughout this journey. I am really grateful to have some extremely supportive friends in my life, especially Mr. Deepanshu Verma, Mr. Diptiman Ghosh, Ms. Kapila Kumawat, Mr. Nand kishor, Mr. Niladri Banerjee, Mr. Raunak Adhikary, Ms. Richa Singh, and Ms. Sapna Mehra. Finally, I would like to express my gratitude to my best friend, Dr. Abhilash Tushir. Your unwavering belief in me, along with the many thoughtful conversations and shared experiences, has helped me navigate the challenges and celebrate the milestones of this journey. Your presence has been a constant source of comfort, motivation, and inspiration, helping me stay focused and resilient throughout this journey.

To everyone who has been part of this journey, your contributions have made a significant impact on the completion of this thesis. Thank you for your encouragement, support, and understanding.

Mansi Mishra